

" I " and his angular speed ω_i . The product " $I\omega_i$ " is the angular momentum which remains constant. When he pulls the dumbbells towards his chest, his moment of inertia ' I_2 ' decreases. Now he spins faster as ' ω_f ' increases to keep ' $I_2\omega_f = \text{constt.}$

Q. 5.13 :- A geo-stationary satellite covers 120° of longitude, so the whole of the Earth's surface for global transmission can be covered by three correctly positioned geo-stationary satellites.

NUMERICAL PROBLEMS

Note :- The solutions to the numerical problems are given below. For problems see last page.

P. 5.1 :- As given :- Diameter of beam = arc length = $s = 2.5 \text{ m}$,
Distance of moon = radius of circle = $r = 3.8 \times 10^8 \text{ m}$,
 $\theta = ?$ Using: $s = r\theta$, $\theta = \frac{s}{r} = \frac{2.5}{3.8 \times 10^8}$
 $\therefore \theta = 6.6 \times 10^{-9} \text{ rad.}$

P. 5.2 :- As given :- Initial angular velocity = $\omega_i = 0$
Final angular velocity = $\omega_f = 45 \text{ rev/min}$

$$\dots \text{ or } \omega_f = \frac{45 \times 2\pi}{60} = \frac{45 \times 2 \times 3.14}{60}$$

$$\therefore \omega_f = 4.71 \text{ rad s}^{-1}$$

$$t = 1.6 \text{ s}, \alpha = \text{ang. acc.} = ?$$

$$\text{using the eq. } \omega_f = \omega_i + \alpha t$$

$$\text{Putting values: } 4.71 = 0 + \alpha(1.6) \Rightarrow \alpha = \frac{4.71}{1.6}$$

$$\therefore \alpha = 2.94 \text{ rad s}^{-2}$$

P. 5.3 :- As given: Moment of Inertia $I = 0.8 \text{ kg m}^2$

Constant Angular velocity $\omega = 100 \text{ rad s}^{-1}$

(i) Angular momentum $L = ?$

(ii) Torque $= ?$

→ (i) Using the eq. $L = I\omega = 0.8 \times 100 \text{ kg m}^2 \text{ s}^{-1}$

$$\text{or } L = 80 \text{ kg m}^2 \text{ s}^{-1} \times \frac{s}{s} = 80 \text{ kg m}^2 \text{ s}^{-1} \times m \times s$$

$$\therefore L = 80 \text{ Nm s} = 80 \text{ Js}$$

→ (ii) $\because \tau = I\alpha$, but as ' ω ' is constant,

$$80 \alpha = 0, \therefore \tau = 0$$

P. 5.4 :- As given :- $m = 5 \text{ kg}$, $F = 0.6 \text{ N}$,

$$r = 0.2 \text{ m}, \alpha = 90^\circ (\because \vec{r} + \vec{F})$$

(i) $\tau = ?$, (ii) $\alpha = ?$

→ (i) using relation: $\tau = rF \sin\alpha$

$$\text{Putting values : } \tau = 0.2 \times 0.6 \times \sin 90^\circ = 0.12 \text{ Nm}$$

$$\therefore \tau = 0.12 \text{ Nm}$$

→ (ii) using the relation: $\tau = I\alpha$

$$\text{but: } I = \frac{1}{2}mr^2, \therefore \tau = \frac{1}{2}mr^2\alpha$$

$$\text{Putting values: } 0.12 = \frac{1}{2} \times 5 \times (0.2)^2 (\alpha)$$

$$0.12 = 0.1(\alpha) \Rightarrow \alpha = \frac{0.12}{0.1} = 1.2 \text{ rad/s}^2$$

$$\therefore \alpha = 1.2 \text{ rad s}^{-2}$$

P. 5.5 :- As given :- $M = 2 \times 10^{30} \text{ kg}$, $R = 7 \times 10^5 \text{ km} = 7 \times 10^8 \text{ m}$,

$$T = 20 \text{ days} = 20 \times 86400 = 1.728 \times 10^6 \text{ s}$$

(i) $L = ?$ (ii) $K.E_I = ?$

→ (i) using eq. $L = I\omega$, where $I = \frac{2}{5}MR^2$ for a sphere, because heavenly bodies are considered as

Spheres. Therefore: $L = \frac{2}{5} MR^2 \times \frac{2\pi}{T}$ ($\because \omega = \frac{2\pi}{T}$)
 Putting values: $L = \frac{2}{5} \times 2 \times 10^{30} \times (7 \times 10^8)^2 \times \frac{2 \times 3.14}{1.728 \times 10^6}$
 $\therefore L = 1.42 \times 10^{42} \text{ kg m}^2 \text{ s}^{-1}$.

$$-(ii) \rightarrow \therefore K.E. = \frac{1}{2} I \omega^2 = \frac{1}{4} \times \frac{2}{5} M R^2 \times \left(\frac{2\pi}{T}\right)^2$$

Putting values: $K.E. = \frac{1}{5} \times (2 \times 10^{30}) \times (7 \times 10^8)^2 \times \left(\frac{2 \times 3.14}{1.728 \times 10^6}\right)^2$
 $\therefore K.E. = 2.59 \times 10^{36} \text{ J}$.

P.5.6 :- As given: $m = 1000 \text{ kg}$, $v = 144 \text{ km/hr}$
 or $v = 144 \times \frac{1000}{3600} = 40 \text{ m/s}$, $r = 100 \text{ m}$,

$$F_c = ?$$

Using the relation: $F_c = \frac{mv^2}{r} = \frac{1000 \times (40)^2}{100} = 16000 \text{ N}$
 $\therefore F_c = 16000 \text{ N} = 1.6 \times 10^4 \text{ N}$.

P.5.7 :- As given: $r = 1000 \text{ m}$, $v = ?$, $g = 9.8 \text{ m/s}^2$.
 Using the relation: $T + W = \frac{mv^2}{r}$ (at highest pt.)
 \therefore for a plane $T = 0$ (no string, no tension).
 $\therefore 0 + mg = \frac{mv^2}{r} \Rightarrow mg = \frac{v^2}{r}$
 or $v = \sqrt{gr} = \sqrt{9.8 \times 1000} = 98.99 = 99 \text{ m/s}$
 $\therefore v = 99 \text{ m/s}$.

P.5.8 :- As given: Radius of moon = $r_m = 1.74 \times 10^6 \text{ m}$,
 Distance between Earth and Moon = $r = 3.85 \times 10^8 \text{ m}$,

L_s = spin angular momentum,
 L_o = orbital " " " , $\frac{L_s}{L_o} = ?$

$$\therefore L_s = I \omega = \frac{2}{5} m r_m^2 \omega, L_o = m r^2 \omega$$

$$\Rightarrow \frac{L_s}{L_o} = \frac{\frac{2}{5} m r_m^2 \omega}{m r^2 \omega} = \frac{\frac{2}{5} (r_m^2)}{r^2} = \frac{\frac{2}{5} \times (1.74 \times 10^6)^2}{(3.85 \times 10^8)^2}$$

$$\therefore \frac{L_s}{L_o} = 8.17 \times 10^{-6}$$
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